

include all units and directions

Kinematics:

$$\Delta \vec{d} = \vec{v}_{av} \Delta t$$

$$\Delta \vec{v} = \vec{a}_{av} \Delta t$$

$$\vec{v}_{av} = \frac{\vec{v}_1 + \vec{v}_2}{2}$$

$$\vec{v}_2 = \vec{v}_1 + \vec{a} \Delta t$$

$$\Delta \vec{d} = \left(\frac{\vec{v}_1 + \vec{v}_2}{2} \right) \Delta t$$

$$\Delta \vec{d} = \vec{v}_1 \Delta t + \frac{1}{2} \vec{a} (\Delta t)^2$$

$$\vec{v}_2^2 = \vec{v}_1^2 + 2a\Delta d$$

Circular Forces:

$$a_c = \frac{v^2}{r} = \frac{4\pi^2 r}{T^2} = 4\pi^2 r f^2$$

$$\sum F = \frac{mv^2}{r} = \frac{4\pi^2 mr}{T^2} = 4\pi^2 m r f^2$$

$$\text{InLoop} : v = \sqrt{3gr} \dots \dots \dots v_{old} = 1.4v_{new}$$

Banked Curve:

$$F_a = F_g \tan \theta$$

$$g \tan \theta = a$$

$$v = \pm \sqrt{g \tan \theta r}$$

$\theta = \text{angle of bank}$

Friction:

$$\mu_s = \frac{F_s}{F_N}$$

$$\mu_k = \frac{F_k}{F_N}$$

Projectile Motion

$$\text{Ground.Level} : \Delta y = \Delta t (v_y - 4.9 \Delta t)$$

$$\text{Other} : 0 = -4.9t^2 + v_y t - \Delta y$$

Acceleration

$$F_{app} - F_f = ma$$

Forces:

$$\vec{F}_g = mg$$

$$\vec{F}_{net} = ma$$

$$F_g = \frac{Gm_1 m_2}{r^2} = \frac{m_s v^2}{r}$$

$$G = 6.67 \times 10^{-11}$$

Uniform Motion : $F_f = F_{app}$

$$F_x = \cos \theta F_{app}$$

$$F_y = \sin \theta F_{app}$$

Curve:

$$F_{app} = F_f = mg\mu_k$$

$$v = \sqrt{\frac{F_{app} \times r}{m}}$$

Coefficient of Friction:

Static :

$$F_{app} = F_f$$

Kinetic :

$$F_{app} - F_{net} = F_f$$

Tension:

$$T_{1y} = T_1 \cos \theta$$

$$T_{2y} = T_2 \cos \theta$$

$$F_g = T_{1y} + T_{2y}$$

Inclined Plane:

Down :

$$F_{app} = F_g \sin \theta$$

$$F_{net} = F_{app} - F_f$$

Up :

$$F_f = mg \cos \theta \times \mu$$

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Work:

$$W = F\Delta d$$

$$W = F(\cos\theta)\Delta d$$

$$W_{with,friction} = F_{net}\Delta d$$

$$W_{total} = \Delta E_k$$

Energy:

$$\Delta E_g = mgh$$

$$E_k = \frac{1}{2}mv^2$$

$$W = \Delta E_k = \frac{1}{2}m(v_f^2 - v_i^2)$$

$$E_{th} = F_k \Delta d$$

Conservation of Energy:

$$mgh + \frac{1}{2}mv^2 = mgh' + \frac{1}{2}mv'^2$$

Elastic Potential Energy:

$$F = -kx(\text{stretched})$$

$$F = kx(\text{compressed})$$

$$E_e = \frac{1}{2}kx^2$$

Frictionless Simple Harmonic Motion:

$$a_c = \frac{4\pi^2 r}{T^2}$$

$$T = 2\pi\sqrt{\frac{m}{k}}$$

$$f = \frac{1}{T}$$

$$A = \frac{-k}{mx}$$

Momentum:

$$\vec{p} = m\vec{v}$$

$$\Delta\vec{p} = m(\vec{v}_2 - \vec{v}_1)$$

$$\Delta\vec{p} = \sum \vec{F}\Delta t$$

$$\vec{p}_{total} = m_1\vec{v}_1 + m_2\vec{v}_2$$

$$m_1\Delta\vec{v}_1 = -m_2\Delta\vec{v}_2$$

$$m_1v_1 + m_2v_2 = m_1v_1' + m_2v_2'$$

$$\frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2 = \frac{1}{2}m_1v_1'^2 + \frac{1}{2}m_2v_2'^2$$

$$\text{elastic hitting stationary} : v_1' = \left(\frac{m_1 - m_2}{m_1 + m_2}\right)v_1$$

$$F\Delta t = m\Delta v$$

$$e = \frac{v_2' - v_1'}{v_1 - v_2}$$

Kepler's Law

$$v = \sqrt{\frac{GM}{r}}$$

$$C = \frac{r^3}{T^2} = \frac{GM}{4\pi^2}$$

$$E_T = E_K + E_g = -\frac{GM_E m}{r_E}$$

$$\Delta E_g = \left(-\frac{GMm}{r_2}\right) - \left(-\frac{GMm}{r_1}\right)$$

$$v = \sqrt{\frac{2GM_E}{r_E}} = \sqrt{\frac{2E_K}{m}}$$